In [1]: use Physics::Unit; use Physics::Measure :ALL; In [2]: # reset rounding \$Physics::Measure::round-val = Nil; OPTION A: lm²(SOUTH-FACING) OPTION B: SOLAR ENERGY TIP: TO MAXIMIZE SUN EXPOSURE, ALWAYS ORIENT YOUR PANELS DOWNWARD AND INSTALL THEM ON THE SURFACE OF THE SUN. Option A - on the roof To break this down into pieces, we have: In [3]:  $\#(0.20 \ \$/kWh) * ((4kWh/m2) per day) * (1 m2) * 20%$ [1] [5] Out[3]: () In [4]: #[1] Dollars per kWh # First we need to create a custom Unit and a custom Measure type # we do not have currency units (yet) so I will ignore the USD currency in the definition Unit.new(defn => '1 / kWh', names => ['\$/kWh']); #dd GetUnit('\$/kWh'); # And a new custom measurement type... class DollarPerKWH is Measure { has \$.units where \*.name eq ('\$/kWh').any; # And then link them with Get Measurement Unit... GetMeaUnit('\$/kWh').NewType('DollarPerKWH'); my  $$\cos t-per-kwh = \Omega'0.2 $/kWh';$ 0.2\$/kWh Out[4]: my \$energy-per-area =  $(\Omega'4 \text{ kWh/m2'});$ 4kWh/m2 Physics::Measure::Insolation my \$power-per-area-on-roof = \$energy-per-area / \( \Omega '1 \) day';  $0.000046W/m^2$ Out[7]: In [8]: \$power-per-area-on-roof.units.type; Out[8]: Irradiance In [9]: #[4] we can just do 1 m2 like this... say 2'1 m2'; 1m^2 In [10]: #[5] and a percent % like this... say 20 %'; #libra format 20'' always needs a space between the number and the unit string 20% Putting it all together: my \$earnings-per-year-on-roof = \$cost-per-kwh \* ( \$power-per-area-on-roof \* ♀ '1 m2' ) \* ♀ '20 %' \* ♀ '1 year'; 58.44① Out[12]:

## In [5]: #[2] Insolation Out[5]: In [6]: \$energy-per-area.^name; In [7]: *#[3] Irradiance*

# the ① indicates that the result is dimensionless

Option B - on the sun

To break this one down into pieces, we have:

[2]

[3]

[4]

# and we can auto normalize SI units to the best SI prefix

[5]

### [1] Out[13]: ()

### In [14]: # set rounding to cope with big values \$Physics::Measure::round-val = 100;

Out[14]: In [15]: | #[2] we can use the postfix style for SI units my \$solar-luminosity = 3.828e26W; 38280000000000026004684800W

In [16]: \$solar-luminosity.norm; Out[16]: In [19]: #[3] and the area (also from https://en.wikipedia.org/wiki/Sun)

Out[15]:

609000000000000000m^2 Out[19]: In [20]: \$solar-area.in: <peta m2>; 6100peta m2 Out[20]:

In [22]: #combining [2] and [3] gives:

\$solar-area.in: <m2>;

my  $solar-area = \Omega'6.09e12 km2';$ 

my \$power-per-area-on-sun = \$solar-luminosity / \$solar-area; 62857100W/m<sup>2</sup> Out[22]: \$power-per-area-on-sun.in: <kW/m^2>;

62900kW/m<sup>2</sup>

Putting it all together:

my \$earnings-per-year-on-sun = \$cost-per-kwh \* ( \$power-per-area-on-sun \* 2'1 m2' ) \* 2'20 %' \* 2'1 year'; 79344822857100(1) Out[25]: In [26]: (\$earnings-per-year-on-sun.value / 1\_000\_000\_000\_000).fmt("%d billion USD per year"); Out[26]: 79 billion USD per year

Out[23]:

Conclusion (I) The sharp eyed reader will note that I then felt duty bound to double check my result, since this is adrift of the 22 million USD per year in Randall's comic. In [52]: # To review the calcs, I thought an order of magnitude approach would help:

sub order-of-magnitude(\$number is copy) { return Nil if \$number == 0; # Order of magnitude undefined for 0 return floor(log10(\$number).Int); &order-of-magnitude Out[52]:

Out[53]: 26

Out[54]: 18

Out[55]: 7

Out[59]:

Out[58]: -4

Out[68]:

Out[69]: 12

Out[72]: 12

Out[73]: True

Out[76]:

Out[71]: 1357714285700①

my \$Lsol-oom = order-of-magnitude( +\$solar-luminosity );

In [54]: my \$Asol-oom = order-of-magnitude( +( \$solar-area.in: <m2> ) );

( \$ppa-sun-oom - ( \$Lsol-oom - \$Asol-oom ) ) <= 1;</pre>

• the main driver of the result is then the power-per-area

In [59]: # check if oom calc is close enough

In [58]: # get oom for ppa sun vs ppa roof

In [71]: # get oom for epy sun vs ppa roof

In [73]: # check if oom calc is close enough

In [74]: dd \$power-per-area-on-sun;

, error => Error)

In [75]: dd \$power-per-area-on-roof;

, error => Error)

1357714285714.286

Conclusion (II)

In [76]: 62857142.85714286e0 / <1/21600>

1357714285700①

my \$ppa-sun-oom = order-of-magnitude( +\$power-per-area-on-sun );

my \$ppa-roof-oom = order-of-magnitude( +\$power-per-area-on-roof );

In [69]: my \$sun-roof-power-ratio-oom = order-of-magnitude( +\$sun-roof-power-ratio );

In [72]: my \$sun-roof-epy-ratio-oom = order-of-magnitude( +\$sun-roof-epy-ratio );

( \$sun-roof-epy-ratio-oom - \$sun-roof-power-ratio-oom ) <= 1;</pre>

my \$sun-roof-power-ratio = \$power-per-area-on-sun / \$power-per-area-on-roof;

my \$sun-roof-epy-ratio = \$earnings-per-year-on-sun / \$\$earnings-per-year-on-roof;

• can also visually check "under the hood", and extract the ratio of value by hand since the units are the same:

dims => [0,1,-3,0,0,0,0,0], dmix => ("W"=>1,"m"=>-2).MixHash, names =>  $['W/m^2']$ );

dims => [0,1,-3,0,0,0,0,0], dmix => ("W"=>1,"m"=>-2).MixHash, names =>  $['W/m^2']$ );

So, I would say, that the right answer is 79 billion USD per year and that my math beats Randall's.

So, PLEASE do feel free to check my results and let me know what you think!

BUT - I am too conscious that I may have made an error - either in these calcs or in the Physics::Measure code.

Irradiance \$power-per-area-on-sun = Physics::Measure::Irradiance.new(value => 62857142.85714286e0, units => Unit.new(factor => 1, offset => 0, defn => 'W / m^2', type => Irradiance,

Irradiance \$power-per-area-on-roof = Physics::Measure::Irradiance.new(value => <1/21600>, units => Unit.new(factor => 1, offset => 0, defn => 'W / m^2', type => Irradiance,

In the spirit of check your results and show your workings I think I am partly protected by the grammar school code of Physics marking ... perhaps this only warrants 6/10 if the result is wrong!

• since many factors are invariant \$cost-per-kwh,  $\Omega$ '1 m2',  $\Omega$ '20 %',  $\Omega$ '1 year' we can set them aside